# Reaction Paths of the $[2+2]$ Cycloaddition of $X=C=Y$ Molecules ( $X, Y=S$ or $\mathbf{O}$ or $\mathbf{C H}_{2}$ ). Ab Initio Study 

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#### Abstract

The reaction paths of $[2+2]$ cycloaddition of the $\mathrm{X}=\mathrm{C}=\mathrm{Y}$ cumulenes were modeled at the MP2/aug-ccpVDZ level. Cycloadditions of allene and $\mathrm{CO}_{2}, \mathrm{CS}_{2}$, or OCS lead in part to the same four-membered products as dimerizations of either ketene or thioketene or addition of ketene and thioketene, respectively. All the reactions studied are concerted and mostly asynchronous. The majority of the allene cycloadditions studied are endoergic and proceed with much higher activation barriers than do the alternative (thio)ketene additions. In comparison with the energy of the substrates, the four-membered cycles incorporating S -atoms are stabilized more than the analogous structures with O -atoms built into the rings. There are also some products that are thermodynamically disfavored, yet seem to be obtainable thanks to a relatively low barrier of the reaction. The AIM analysis of the electron density distribution in the transition state structures allowed distinguishing pericyclic from pseudopericyclic and nonplanar-pseudopericyclic types of reaction.


## Introduction

Four-membered heterocycles are of concern for today's chemistry. Introduction of heteroatoms into a small ring produces significant changes in charge distribution and ring strain of the whole molecule. ${ }^{1}$ Usually, heterocyclic fourmembered rings are thermally unstable and highly reactive. Therefore, they are desirable products as well as building blocks for further syntheses. 2-Oxetanones (a, Scheme 1) considered, inter alia, in this paper have stimulated considerable interest in the pharmaceutical community owing to their potent biological activity spectrum ranging from enzyme inhibition to viral inactivation as well as pancreatic lipase inhibitors, which are supposed to be responsible for obesity. ${ }^{1}$ 2-Oxetanones have also been utilized as herbicides and even as educts for preparing polymeric materials. ${ }^{1}$ Among 2-oxetanones, diketene (4-meth-ylene-2-oxetanone; $\mathbf{b}$, Scheme 1) is a reactive and versatile compound that is used for introducing functionalized $\mathrm{C}_{2}, \mathrm{C}_{3}$, and $\mathrm{C}_{4}$ units into organic compounds. ${ }^{2}$ Diketene has been also reported to be a potent bactericide useful for disinfecting large areas. ${ }^{2}$ 3-Oxetanones (c, Scheme 1) also exhibit biological activity. ${ }^{3}$ Numerous steroids incorporating the 3-oxetanone ring exhibit anti-inflammatory and anti-glucocorticoid activity, whereas some of them act as oral diuretics. ${ }^{4}$ In the presence of a base, 3 -oxetanones are unstable and slowly polymerize to give a highly viscous material, presumably polyoxetanone $\left[-\mathrm{CH}_{2} \mathrm{C}(\mathrm{O})-\mathrm{CH}_{2}-\mathrm{O}-\right] .{ }^{5}$

The chemistry of sulfur analogues of oxetanones has been less developed. However, in the group of compounds, $\beta$-propiothiolactones (d, Scheme 1) are used in commercial polymerization and also in laboratory preparation of macrocyclic thiolactones which were demonstrated to exhibit supramolecular properties. ${ }^{6}$ The isomers of diketene and its sulfur analogue are

[^0]known, too. The compounds with two heteroatoms built into the ring exhibit interesting properties. The most known are 1,2dioxetanes (e, Scheme 1), whose chemiluminescent properties have found extensive application in emergency lighting, traffic control, and sports products (lightening golf balls, hockey pucks), ${ }^{7}$ as well as in bioanalytical and clinical chemistry for the determination of biomolecules, DNA fingerprinting and sequencing, reporter gene assays, virus detection, and microbe screening. ${ }^{1,8}$ In the group of compounds with two sulfur atoms built into the ring, substituted 1,3-dithietanes (f, Scheme 1), when directly attached, increase the activity of cephalosporins. ${ }^{1}$ On the other hand, the 2-ylidene derivative (known as YH439) inhibits the mutagenicity and tumorigenicity of vinyl carbamate in liver; hence it has been proposed as a new hepatoprotective agent. ${ }^{9}$ Also, methylene substituted dithietanes are antibiotics active against Gram-negative bacteria, and some of them are claimed to be fungicides and drugs decreasing hyperglycemia. Imino 1,3-dithietanes are very useful synthetic pesticides and fungicides. ${ }^{1}$ Many derivatives of 1,3-dithietane are used as plasticizers in the production of poly(vinyl chloride) or as monomers in the preparation of polyester coatings. ${ }^{1}$

A $[2+2]$ cycloaddition of $\pi$-electron compounds is potentially an attractive, straightforward way for obtaining the four-membered heterocycles (Scheme 2). ${ }^{1}$ The ketene $[2+2]$ cycloaddition (dimerization), which serves as a kind of reference reaction in this paper, has been studied by both experimental ${ }^{10}$ and theoretical ${ }^{11,12}$ methods. In 1934, kinetic studies revealed that diketene dimerization does not proceed through a biradical intermediate. ${ }^{10 \mathrm{a}}$ The above was confirmed in 1943 by studies on diketene pyrolysis. ${ }^{10 \mathrm{~b}}$ Since the mid-1950s, it has been known that diketene is the main product of the dimerization; however, in the case of dimerization of substituted ketenes, derivatives of cyclobutadione may be the preeminent product. ${ }^{2}$ The ketene dimerization activation barrier, found experimentally for the gas phase, is equal to $31 \mathrm{kcal} / \mathrm{mol},{ }^{10 \mathrm{~b}}$ and calculated at the SCF/ $\mathrm{DZ}+\mathrm{P}$ level is equal to $32 \mathrm{kcal} / \mathrm{mol}$ (probably by chance). ${ }^{12}$ 1,3-Cyclobutanedione, a potential ketene dimerization product,

## SCHEME 1: Examples of Four-Membered Ring Compounds Important to Pharmacy and Chemical Industry ${ }^{a}$


a

b


C

d

e

f
${ }^{a}$ Compounds: a, 2-oxetanones; b, diketene; c, 3-oxetanones; d, $\beta$-propiothiolactones; $\mathbf{e}, 1,2$-dioxetanes; $\mathbf{f}, 1,3$-dithietanes.

## SCHEME 2: Possible Product Structures Obtained from [2 +2$]$ Cycloaddition of Cumulene Structures Considered



SCHEME 3: Orbital Arrangement of Two Ketene Molecules Allowed by the Woodward-Hoffmann Rules for the $\left[\boldsymbol{r}_{\boldsymbol{s}}+\right.$ $\boldsymbol{\pi}^{2}$ ] Cycloaddition Reactions Leading to Diketene (top) and 1,3-Cyclobutadinone (bottom)


OR

requires a $36 \mathrm{kcal} / \mathrm{mol}$ barrier to be overcome ${ }^{12}$ and usually is not formed in detectable amounts. The structure of the transition state toward diketene formation, found at the SCF level, ${ }^{12}$ indicated a nonsynchronous reaction with partial formation of one $\sigma$-bond and partial breakage of two $\pi$-bonds. The nonsynchronous reaction mechanism was also calculated for the pathway leading to 1,3 -cyclobutanedione, though the product is a symmetrical molecule. The activation barriers for formation of diketene, 1,3-cyclobutanedione, and 2,4-dimethylene-1,3dioxetane, calculated at the MP2/4-31G* level, were found to be equal to $29.8,35.1$, and $61.2 \mathrm{kcal} / \mathrm{mol}$, respectively. ${ }^{12}$ Quite recent studies, performed at the MP2/6-31G*, MP4/6-31G*// MP2/6-31G*, and $\operatorname{CCSD}(\mathrm{T}) / 6-31 \mathrm{G}^{*}$ levels, yielded transition state (TS) structures fairly similar to that of ref 12 ; however, the $\operatorname{CCSD}(\mathrm{T})$ calculations suggested 1,3-cyclobutanedinone to be the main product favored by the lowest reaction energies of both the ground and TS states. ${ }^{13}$ It seems that, until now, the mechanism of the diketene formation has not been established unequivocally.

The early reaction mechanism concepts were based on the Woodward-Hoffmann (W-H) orbital symmetry conservation rules. ${ }^{14}$ To apply the rules, there must be a symmetry element intersecting the newly forming bonds and the process must be concerted (i.e., must proceed in one step). The $\mathrm{W}-\mathrm{H}$ rules have recently been criticized. ${ }^{15-17}$ If one molecule is in an excited state, it is geometrically different from the other, the system loses symmetry, and the rules are no longer valid. ${ }^{15}$ Studies on the simplest example for which the supra-antra $\left[\pi 2_{\mathrm{s}}+{ }_{\pi} 2_{\mathrm{a}}\right.$ ]
mechanism must be obeyed, the ethene cycloaddition, show that this is a stepwise (i.e., multistep) reaction rather than a concerted process. ${ }^{16}$ Moreover, an attempt to find the ethene cycloaddition transition state corresponding to the $\left[\pi 2_{\mathrm{s}}+{ }_{\pi} 2_{\mathrm{a}}\right]$ mechanism has failed: instead of first order, the second-order saddle point was found to occur at the MC-SCF level. ${ }^{17}$ Although the presence of a heteroatom excludes the existence of a symmetry element intersecting the newly forming bonds, for the ethene-ketene and ketene-ketene $[2+2]$ cycloadditions, Woodward and Hoffman had proposed the $\left[{ }_{\pi} 2_{\mathrm{s}}+{ }_{\pi} 2_{\mathrm{a}}\right.$ ] mechanism. ${ }^{14}$ According to the rules, in the ketene dimerization the two ketene molecules should be placed either in parallel or in perpendicular planes (Scheme 3). For the ketene dimerization, attempts at finding the TS structures meeting the $\mathrm{W}-\mathrm{H}$ rules has failed. ${ }^{12}$ In the pathway leading to 1,3 -cyclobutanedinone, the structures corresponding strictly to the rules for the $\left[{ }_{\pi} 2_{\mathrm{s}}+{ }_{\pi} 2_{\mathrm{s}}\right.$ ] addition, possessing $C_{2 h}$ symmetry, exhibited four imaginary frequencies instead of one characterizing TS, whereas the structure corresponding to the $\left[\pi_{\mathrm{s}}+{ }_{\pi} 2_{\mathrm{a}}\right]$ pathway exhibited two imaginary frequencies. ${ }^{12}$ Therefore, for ketene dimerization, the $\left[\pi_{\mathrm{s}}+{ }_{\pi} 2_{\mathrm{s}}+{ }_{\pi} 2_{\mathrm{s}}\right]$ concerted pathway with three $\pi$-bonds incorporated and unsymmetrical TS has been recognized. ${ }^{12,18}$

Now, the cycloaddition reactions are analyzed in terms of pericyclic and pseudopericyclic types of reaction rather than the Woodward-Hoffmann rules. ${ }^{14}$ The $\mathrm{W}-\mathrm{H}$ rules were formulated only for pericyclic reactions. A pericyclic reaction is concerted and takes place on a closed curve. ${ }^{14}$ The transition
structures of pericyclic reactions are expected to be highly nonplanar.

According to the original Ross, Seiders, and Lemal's papers ${ }^{19}$ in which the term "pseudopericyclic reaction" was introduced, "a pseudopericyclic reaction is a concerted transformation whose primary changes in bonding compass a cyclic array of atoms, at one (or more) of which nonbonding and bonding atomic orbitals interchange roles. In a crucial sense, the role interchange means a 'disconnection' in the cyclic array of overlapping orbitals because the atomic orbitals switching functions are mutually orthogonal". In that paper, ${ }^{19 a}$ a $[1,3]$ sigmatropic reaction was analyzed and a lone pair was transformed into a single bond, and at the same time another single bond was transformed into another lone pair. This occurred in a "cyclic array of atoms".

For nearly 20 years, pseudopericyclic reactions did not attract much attention. In the mid-1990s Birney first, ${ }^{20}$ and later several other authors, ${ }^{21-25}$ revived their interest in them and showed that a number of organic syntheses follow this type of process. Birney and co-workers concluded that in the pseudopericyclic reactions the TS structure (1) is planar (or nearly planar), (2) exhibits orbital disconnections, and (3) determines relatively low activation barrier; additionally, (4) pseudopericyclic reactions are orbital symmetry allowed.

The pseudopericyclic reaction is studied by using two main treatments: the atomic and molecular orbital formalism [Lemal, ${ }^{19}$ Birney $^{20}$ ] and the electron density concept [Chamorro, ${ }^{24}$ Lopez $^{25}$ ]. In 2003, Chamorro used the electron localization function (ELF) method to study exactly the same reactions as Birney, ${ }^{20 \mathrm{~b}}$ in which atomic and molecular orbital methodology was used. The conclusions of both studies were identical. It is crucial that, in the ELF methods, the concept of "disconnection" involved in an orbital framework was replaced by detecting disconnections via examination of direct electron fluctuation at the interaction centers.

The atoms-in-molecules (AIM) method used in this paper is equivalent to the ELF method used by Chamorro. A minor difference between the methods consists of the fact that, in the AIM theory, electron density basins are associated with "atoms", whereas in the ELF approach they are associated with "pair regions". The absence of a bond in the AIM method is connected to the lack of the bond critical point (BCP), whereas in the ELF method negligible electron exchange between the basins is associated with appropriate "pair regions".

Quite recently, López et al. ${ }^{25}$ have used successfully AIM analysis to study pericyclicity and pseudopericyclicity of electrocyclic reactions. In particular, López et al. showed the ellipticity of the BCP to be a very useful tool in classification of the reaction mechanisms. As stated by López et al., ${ }^{25}$ electron density is a physical observable; therefore, by using them one avoids any arbitrary processing of the wave functions such as orbital localization (and replacement of molecular orbitals by an arbitrary and illustrative, yet oversimplified, atomic orbital picture). It is also thought that the analysis based on the localized orbitals may not be fully adequate to describe TS structures whose orbitals are essentially diffused.

It can be summarized that, until now, to differentiate the pseudopericyclic from the pericyclic type of reactions, the following approaches were used: the natural bond analysis (NBO) of the TSs, ${ }^{20,21}$ magnetic properties and aromaticity of the TSs, ${ }^{22,23}$ anisotropy of the current induced density (ACID) analysis, ${ }^{23}$ electron localization function (ELF), ${ }^{24}$ and ellipticity of AIM determined critical points. ${ }^{25}$

Motivation for the present study originates from contemplation of a potential applicability of $\mathrm{CO}_{2}$, the industrial waste and
pollutant, addition to allene $\left(\mathrm{CH}_{2}=\mathrm{C}=\mathrm{CH}_{2}\right)$ that would lead to the industrially desirable product: diketene. The reaction was found to be thermodynamically disfavored. ${ }^{26}$ However, it is known that, at high pressure of $\mathrm{H}_{2}$ and in the presence of a $\left[\mathrm{RhCl}\left(\mathrm{C}_{2} \mathrm{H}_{4}\right)\left(\mathrm{P}^{\mathrm{i}} \mathrm{Pr}_{3}\right)\right]_{2}$ catalyst, 3-methylene-2-oxetanone is formed from $\mathrm{CO}_{2}$ and allene. ${ }^{27}$ Thus, the reaction barrier appeared to be substantial, and the present study stems from this very problem. Because thioketene was reported to be even more reactive than ketene, ${ }^{28}$ we extended the study to cover sulfur analogues of $\mathrm{CO}_{2}$ and ketene cycloaddition reactions. In fact, we consider cycloaddition leading to all possible four-membered cycle product molecules containing two heteroatoms, either O or S or both. To this aim, we performed the MP2/aug-cc-pVDZ calculations of the reactants, TS structures, and reaction products. The atoms-in-molecules (AIM) ${ }^{29}$ analysis of critical points of the electron density in the TSs allowed us to find arguments for a distinction between pericyclic, pseudopericyclic, and nonplanar (NP)-pseudopericyclic type of reactions.

This paper is organized as follows: First, we compare the [2 $+2]$ addition reaction of $\mathrm{CO}_{2}$ and allene with ketene dimerization. Second, the analogous comparison is made for the $\mathrm{CS}_{2}$ and thioketene reactions. Third, the OCS and allene additions are compared with the additions of thioketene and ketene. Next, the energetic and geometry regularities are summarized. Finally, reaction mechanisms are discussed in terms of the AIM method.

## Calculations

The ab initio MP2/aug-cc-pVDZ calculations ${ }^{30,31}$ were performed by using Gaussian 98 and Gaussian 03 packages of programs. ${ }^{32}$ The transition structures were found by using the quadratic synchronous transit-guided quasi-Newton (QST3) method developed by Schlegel and co-workers, which uses a quadratic synchronous transit approach to get closer to the quadratic region around the transition state, and then uses a quasi-Newton or eigenvector-following algorithm to complete the optimization. ${ }^{33}$ As for minimizations, it performs optimizations by default by using redundant internal coordinates. ${ }^{34}$ For the lowest reaction barriers the intrinsic reaction coordinate (IRC) calculations ${ }^{35}$ were performed for both the forward and reverse directions of the vibrational mode calculations to confirm that the transition states found connect the appropriate minima.

The G3 method ${ }^{36}$ was used when the energies of two structures were almost equal. The G3 calculations are composed of several stages (the MPBT calculations corrected for a spinorbit term and some higher level corrections for valence electrons) and were shown to yield energy accuracy of 1-2 kcal/mol. ${ }^{36}$

The imaginary vibrations were visualized by using the Molekel 4.0 program. ${ }^{37}$ The bond critical points $(3,-1)$ and the ring critical points $(3,+1)$ in the TS structures were localized by using the AIM2000 program. ${ }^{29 a}$

## Results and Discussion

The [2 + 2] cycloaddition of allene and $\mathrm{CX}_{2}$ (path A ) and the $\mathrm{H}_{2} \mathrm{CCX}$ dimerization (path B) can lead potentially to two and six products, respectively (Figures 1 and 2). The [ $2+2$ ] cycloaddition of allene and OCS (path A) and the $\mathrm{H}_{2} \mathrm{CCO}$ addition with $\mathrm{H}_{2} \mathrm{CCS}$ (path B) can lead potentially to four and eight products, respectively (Figure 3). The Gibbs free energy differences, defining the reaction energies and the activation barriers at 298 K , are presented in Chart $1\left(\mathrm{CO}_{2}+\right.$ allene vs ketene + ketene $)$, Chart $2\left(\mathrm{CS}_{2}+\right.$ allene vs thioketene + thioketene), and Chart 3 (OCS + allene vs ketene + thioketene). Schematic structures, molecule numbering, and names are listed


Figure 1. Atom numbering and selected geometric parameters (angstroms and degrees) of the transition state structures for $\mathrm{CO}_{2}$ and allene cycloaddition (path A) and ketene dimerization (path B) calculated at the MP2/aug-cc-pVDZ level of theory. Values in brackets and braces are taken from refs 12 and 13 , respectively.

A: $\mathrm{CS}_{2}$ +allene addition










$\mathrm{TS}_{\mathrm{s}}$ (XIII)




Figure 2. Atom numbering and selected geometric parameters (angstroms and degrees) of the transition state structures for $\mathrm{CS}_{2}$ and allene cycloaddition (path A) and thioketene dimerization (path B) calculated at the MP2/aug-cc-pVDZ level of theory.
in Table S1 of the Supporting Information (SI). The HOMOLUMO orbital energy gaps for the reactants studied are gathered in Table S2 of SI. All the energetic data are collected in Tables

S3, S4, and S5. They contain also the energetics at 0 K corrected for zero-point energies, and mode specification of imaginary frequencies at the transition states. Additionally, the geometric


Figure 3. Atom numbering and selected geometric parameters (angstroms and degrees) of the transition state structures for OCS and allene cycloaddition (path A) and cycloaddition of ketene with thioketene (path B) calculated at the MP2/aug-cc-pVDZ level of theory.

CHART 1: Energetics $\Delta G(p=1 \mathrm{~atm}, T=298 \mathrm{~K})$ of the $[2+2]$ Cycloaddition Reaction of Allene and $\mathrm{CO}_{2}$ (Path A) and Ketene Dimerization (Path B) Calculated at the MP2/aug-cc-pVDZ Level ${ }^{a}$

${ }^{a}$ The G3 energies are presented in brackets. For numbering of the structures, see Figure 1.
details and energetic data on the products and transition states studied are collected in Tables S6-S11 of SI.

Allene Addition to $\mathbf{C O}_{\mathbf{2}}$ vs Ketene Dimerization. Some products of the $\mathrm{CO}_{2}$ addition to allene, as well as ketene dimerization reaction (Figure 1), were studied by us previously. ${ }^{26}$ Therefore, we place here special emphasis on the transition states. Hereafter, the $\omega$-angle reflects the deformation of the four-membered ring and is defined as the dihedral angle of the $1-2-3-4$ ring atoms.

The previous studies on ketene dimerization ${ }^{12,13}$ have shown that the energy difference between the most stable products I (diketene) and II (1,3-cyclobutanedione) is very sensitive to the computational method applied. This also holds true in our calculations. At the MP2/aug-cc-pVDZ level, structure II seems to be favored both thermodynamically and kinetically, although the energy difference between the molecules I and II equals ca. $1 \mathrm{kcal} / \mathrm{mol}$, a value within the range of accuracy of the computational method used. The activation barrier for $\mathbf{I}$ is equal to $30.1 \mathrm{kcal} / \mathrm{mol}$ and it is in very good agreement with the experimental value ( $31 \mathrm{kcal} / \mathrm{mol}$ ), ${ }^{10 \mathrm{~b}}$ however; in contrast to the experimental findings, the barrier calculated for II is lower than that for I by $1.4 \mathrm{kcal} / \mathrm{mol}$. The reaction paths toward I and II were confirmed by the IRC calculations (Figure S1). To verify the magnitude of the TS energy difference, we recalculated the structures by using the G3 method constructed specially for reaction energetics. As a result, the barrier toward I was lower than that toward II, yet the experimental values were reproduced less accurately than those at the MP2/aug-cc-pVDZ level. Surprisingly, the $\operatorname{CCSD}(\mathrm{T}) / 6-31 \mathrm{G}^{*}$ calculations, assumed to be accurate, have favored formation of II, whereas CCSD/6-31G* and CASSCF have favored I by a lower activation barrier. ${ }^{13}$

The third, still thermodynamically stable product of ketene dimerization, IV (1,2-cyclobutanedione), has never been reported, yet, the unstable product VI (2,4-dimethyleno-[1,3]dioxetane) was a subject of theoretical study ${ }^{11 \mathrm{c}}$ and was shown to be by $30 \mathrm{kcal} / \mathrm{mol}$ less stable than I and II. Although IV is expected to be stable (Chart 1, Tables S3 and S7), the activation barrier leading to $\mathbf{I V}, \mathrm{TS}_{\mathrm{B}}(\mathbf{I V})$, is almost twice as high as $\mathrm{TS}_{\mathrm{B}}(\mathbf{I})$ and $\mathrm{TS}_{\mathrm{B}}(\mathbf{I I})$. The other ketene dimerization products are

CHART 2: Energetics $\Delta G(p=1 \mathrm{~atm}, T=298 \mathrm{~K})$ of the $[2+2]$ Cycloaddition Reaction of Allene and $\mathrm{CS}_{2}$ (Path A) and Thioketene Dimerization (Path B) Calculated at the MP2/aug-cc-pVDZ Level ${ }^{a}$

${ }^{a}$ The G3 energies are presented in brackets. For numbering of the structures, see Figure 2.

CHART 3: Energetics $\Delta G(p=1 \mathrm{~atm}, T=298 \mathrm{~K})$ of the $[2+2]$ Cycloaddition Reaction of Allene and OCS (Path A) and Cycloaddition of Ketene with Thioketene (Path B) Calculated at the MP2/aug-cc-pVDZ Level ${ }^{a}$

${ }^{a}$ For numbering of the structures, see Figure 3.
both thermodynamically unstable and have high activation barriers. The least stable is VII (3,4-dimethyleno-[1,2]-dioxetane), with TS energy high enough to excite one of the ketene molecules to the triplet state during dissociation into two ketenes. The possibility of such an excitation is common to the class of such compounds. ${ }^{38}$

Most of the ketene dimerization reactions are concerted, although they proceed through the TS geometries suggestive of a highly nonsynchronous process (Figure 1). Always
the $\sigma(\mathrm{C}-\mathrm{C})$ bond is formed first and the $\sigma(\mathrm{C}-\mathrm{O})$ next, though the latter is shorter in the product. In TS structures, the differences between $\sigma(\mathrm{C}-\mathrm{C})$ and $\sigma(\mathrm{C}-\mathrm{O})$ distances exceed 0.6 $\AA$ (Table S6). However, $\mathrm{TS}_{\mathrm{B}}(\mathbf{V I})$ constitutes an exception: the two $\sigma(\mathrm{C}-\mathrm{O})$ bonds are formed simultaneously. In this case, the two ketene molecules approach each other in nearly the same plane, the $\mathrm{TS}_{\mathrm{B}}(\mathbf{V I})$ is skewed by $\omega=24^{\circ}$, and the product belongs to the $C_{2 h}$ symmetry point group. Also $\mathrm{TS}_{\mathrm{B}}(\mathbf{V})$ and $\mathrm{TS}_{\mathrm{B}}($ VII $)$ belong to the $C_{2 h}$ and $C_{s}$ groups, respectively.

Lack of symmetry of the $\mathrm{TS}_{\mathrm{B}}(\mathbf{I}), \mathrm{TS}_{\mathrm{B}}(\mathbf{I I})$, and $\mathrm{TS}_{\mathrm{B}}(\mathbf{I V})$ is counterintuitive, because the products belong (nearly) to the $C_{s}$, $D_{2 h}$, and $C_{2 v}$ point groups of symmetry, respectively. This results from the way the molecules approach each other: first, the heavy atoms are not in one plane; second, the planes determined by the $=\mathrm{CH}_{2}$ groups are close to perpendicular. It is noticeable that at the same time these asymmetric TS structures have relatively low energies. Moreover, comparison of the reactants' original geometries shows one of them to be deformed only slightly. Generally, the geometries of $\mathrm{TS}_{\mathrm{B}}(\mathbf{I})$ and $\mathrm{TS}_{\mathrm{B}}(\mathbf{I I})$ calculated here are quite similar to those calculated previously by using the HF and MP2 methods. ${ }^{12,13}$ However, as can be expected, the agreement with the MP2/6-31G* results ${ }^{13}$ is better than that with the HF/DZ+P data. ${ }^{12}$ The previous studies have concluded the ketene dimerization to run by the concerted $\left[\pi 2_{\mathrm{s}}\right.$ $\left.+{ }_{\pi} 2_{\mathrm{s}}+{ }_{\pi} 2_{\mathrm{s}}\right]$ mechanism ${ }^{12}$ instead of the $\left[{ }_{\pi} 2_{\mathrm{s}}+{ }_{\pi} 2_{\mathrm{a}}\right]$ predicted by the Woodward-Hoffmann rules. ${ }^{14}$ The $\mathrm{W}-\mathrm{H}$ rules require one symmetry element to be preserved throughout the entire reaction path, whereas such a constraint leads to the $C_{2}$ symmetry stationary point of second order. ${ }^{12}$ Thus, interaction of three $\pi$-bonds was proposed for the $\mathrm{TS}_{\mathrm{B}}(\mathbf{I})$ : HOMO and LUMO of one molecule and HOMO of the other. ${ }^{12}$ The AIM analysis of critical points in the TSs (presented in more detail in The [2 + 2] Cycloaddition Mechanisms section) suggests, however, that the reaction with $\mathrm{TS}_{\mathrm{B}}(\mathbf{I})$ is pseudopericyclic rather than pericyclic. Thus, neither $\left[2_{\mathrm{s}}+{ }_{\pi} 2_{\mathrm{a}}\right]$ nor $\left[\pi 2_{\mathrm{s}}+{ }_{\pi} 2_{\mathrm{s}}+{ }_{\pi} 2_{\mathrm{s}}\right]$ mechanisms can obey for the reaction since the $\mathrm{W}-\mathrm{H}$ rules cannot be applied for pseudopericyclic reactions.

The reaction that would lead also to the diketene molecule I is [ $2+2$ ] cycloaddition of allene to $\mathrm{CO}_{2}$. Then, the 3-methylene isomer of diketene, III, would be formed, too. However, in this reaction, the two products are thermodynamically disfavored as their reaction energies exceed $14 \mathrm{kcal} / \mathrm{mol}$ (Chart 1, Table S3). Moreover, the activation barriers exceed $60 \mathrm{kcal} / \mathrm{mol}$, although the barrier toward $\mathbf{I}$ is a bit lower than that toward III. Despite the theoretical predictions, the isomer III was obtained as a product of $\mathrm{CO}_{2}$ cycloaddition to allene under a high pressure of $\mathrm{H}_{2}$ and in the presence of $\left[\mathrm{RhCl}\left(\mathrm{C}_{2} \mathrm{H}_{4}\right)\left(\mathrm{P}^{\mathrm{i}} \mathrm{Pr}_{3}\right)\right]_{2}$ as catalyst ${ }^{27}$ (which itself usually breaks the symmetry of the reagents).

The geometries of transition state structures $\mathrm{TS}_{\mathrm{A}}(\mathbf{I})$ and $\mathrm{TS}_{\mathrm{A}}($ III $)$ (Figure 1) are suggestive of concerted and synchronous pathways as the distance differences between the newly created $\sigma(\mathrm{C}-\mathrm{C})$ and $\sigma(\mathrm{C}-\mathrm{O})$ bonds are much smaller than those for path B. However, in the products I and III, the $\sigma(\mathrm{C}-\mathrm{O})$ is shorter than the $\sigma(\mathrm{C}-\mathrm{C})$ distance, whereas the opposite relation is observed to hold for the $\mathrm{TS}_{\mathrm{A}}(\mathbf{I})$ and $\mathrm{TS}_{\mathrm{A}}(\mathbf{I I I})$ structures. Thus, to form $\sigma$-bonds on the way from the TS to the ground state of the product, the C 2 and C 3 atoms traverse a shorter distance than the C 4 and O 1 atoms do. This means that actually the process is asynchronous. $\mathrm{TS}_{\mathrm{A}}(\mathbf{I})$ is rather slightly nonplanar, whereas $\mathrm{TS}_{\mathrm{A}}(\mathbf{I I I})$ is planar, and as shown in The $[2+2]$ Cycloaddition Mechanisms section they are both pericyclic.

Allene Addition to $\mathrm{CS}_{\mathbf{2}}$ vs Thioketene Dimerization. The energetics of thioketene dimerization is quite different from that
of ketene. First, all reactions are exoergic with reaction energies of at least $-14 \mathrm{kcal} / \mathrm{mol}$ (Chart 2, Tables S4 and S9). Second, the lowest activation barrier in the $\mathrm{H}_{2} \mathrm{CCS}$ dimerization is by ca. $10 \mathrm{kcal} / \mathrm{mol}$ lower than the lowest one in the $\mathrm{H}_{2} \mathrm{CCO}$ dimerization, and the highest is equal to $35 \mathrm{kcal} / \mathrm{mol}$ only, whereas in the ketene dimerization it is as high as $90 \mathrm{kcal} / \mathrm{mol}$. We think that the HOMO-LUMO energy gap, smaller for the thioketene than for the ketene dimerization (Table S2), can be an explanation for the barrier lowering.

The MP2 energies for $\mathrm{TS}_{\mathrm{B}}(\mathbf{I X})$ and $\mathrm{TS}_{\mathrm{B}}(\mathbf{X I I})$ are very close to each other (Chart 2, Tables S4 and S9). Therefore, we checked their G3 energies as well as the G3 energy for $\mathrm{TS}_{\mathrm{B}}$ (XIV). Unexpectedly, the latter appeared to be the lowest, whereas this was not the case in the MP2 calculations. Similarly to the ketene dimerization reaction, differences between the MP2 and G3 calculated energies of TSs are significant and reach ca. $8 \mathrm{kcal} / \mathrm{mol}$. There may be two main reasons for such a discrepancy: one is the unsaturation of the basis set used, and the second could be the spin-orbit coupling correction present in the G3 scheme and absent in the direct MP2 calculations.

According to the MP2 calculations, the most stable product of the thioketene dimerization is the disulfur analogue of diketene, IX, which is favored both thermodynamically and kinetically (Chart 2, Tables S4 and S9). Despite the fact that XII is not so stable as IX, its activation barrier is as low as that of IX. Thus, XII can possibly be formed owing to kinetic control. Surprisingly, although the product XIV (3,4-dimeth-ylene-[1,2]-dithietane), with the two neighboring sulfur atoms in the ring, is the least stable product, its activation barrier (21.8 $\mathrm{kcal} / \mathrm{mol})$ is comparable with the lowest barriers: $\mathrm{TS}_{\mathrm{B}}(\mathbf{I X})$ and $\mathrm{TS}_{\mathrm{B}}(\mathbf{X I I})$ (for IRC profiles, see Figure S2). The remaining activation barriers are higher than $29 \mathrm{kcal} / \mathrm{mol}$. Unexpectedly, $\mathrm{TS}_{\mathrm{B}}(\mathbf{X})$ and $\mathrm{TS}_{\mathrm{B}}(\mathbf{X I})$ have the same energy. This is not an accident, because they are mirror images: the deformation angle of the ring, $\omega$, is equal to $58^{\circ}$ in $\mathrm{TS}_{\mathrm{B}}(\mathbf{X})$ whereas in $\mathrm{TS}_{\mathrm{B}}(\mathbf{X I})$ it is $-58^{\circ}$ (Figure 2). It is not quite obvious why this is so. The structure of $\mathrm{TS}_{\mathrm{B}}(\mathbf{X I})$ does not look like one that has converged to the XI product; however, similar TS geometries were obtained by using both the MP2 and G3 models. Thus, we think that, in the course of the reaction between the $\mathrm{TS}_{\mathrm{B}}(\mathbf{X I})$ and $\mathbf{X I}$, rotation around the newly forming $\mathrm{C} 3-\mathrm{C} 2$ bond must have occurred.

Considering the possible mechanisms of thioketene dimerization, we may state that the reactions are concerted and nonsynchronous because they proceed through highly asymmetric transition state structures. In each $\mathrm{TS}_{B}$ structure, the difference between the two newly forming bond distances equals at least $0.8 \AA$ (Figure 2). Even $\mathrm{TS}_{\mathrm{B}}(\mathbf{X I I I})$ is not an exception, though it was expected to be as symmetric as the analogous $\mathrm{TS}_{\mathrm{B}}(\mathbf{V I})$ structure leading to 1,3-dioxetane (Figure 1). The differences in the symmetry of $\mathrm{TS}_{\mathrm{B}}$ (XIII) (2,4-dimethylene-[1,3]-dithietane) and $\mathrm{TS}_{\mathrm{B}}(\mathbf{V I})$ (2,4-dimethylene-[1,3]-dioxetane) are due to differences between the approach of the two ketene and two thioketene molecules. The former come near each other in the antiparallel manner, whereas the arrangement of the latter is antiparallel; however, the plane in which one molecule is contained is rotated through the right angle toward the other plane (Figures 1 and 2). As a result, the ring deformation angle in the former case is equal to ca. $25^{\circ}$, whereas in the latter case it is $0^{\circ}$. Note that in two cases, viz., $\mathrm{TS}_{\mathrm{B}}($ XIII $)$ and $\mathrm{TS}_{\mathrm{B}}($ XIV $)$, one bond has been formed almost completely as being practically equal to those in the appropriate respective products (Table S8). Ring deformation in $\mathrm{TS}_{\mathrm{B}}$ (XIV) (3,4-dimethylene-[1,2]dithietane) is significant ( $\omega=-62^{\circ}$ ), as compared to zero in $\mathrm{TS}_{\mathrm{B}}(\mathbf{V I I})$-the oxygen analogue of XIV.

In the cycloaddition of allene with $\mathrm{CS}_{2}$, reaction path A , only two products are plausible and their predicted reaction energies are equal to ca. -5 and $-3 \mathrm{kcal} / \mathrm{mol}$ for VIII and IX, respectively (Chart 2). The 3-methylene isomer, VIII, is favored over IX thermodynamically; however, its activation barrier is higher by ca. $4 \mathrm{kcal} / \mathrm{mol}$ than that for the 4 -methylene isomer (Figure S2). Therefore, the latter could perhaps be obtained due to kinetic control. Nevertheless, a catalyst seems to be necessary because the activation barriers exceed $50 \mathrm{kcal} / \mathrm{mol}$ and rapid reactions are hardly possible. Similarly to the TS structures found in the allene and $\mathrm{CO}_{2}$ cycloadditions, the $\mathrm{TS}_{\mathrm{A}}(\mathbf{V I I I})$ structure is almost planar, whereas $\mathrm{TS}_{\mathrm{B}}(\mathbf{I X})$ is deformed. The 4-methylenethietane-2-thione TS structure, $\mathrm{TS}_{\mathrm{A}}(\mathbf{I X})$, is much more skewed than is its oxygen analogue, $\mathrm{TS}_{\mathrm{A}}(\mathbf{I}): 70^{\circ}$ vs $20^{\circ}$, respectively. It suggests that, similarly as for diketene, in the course of the reaction leading to IX, the molecules approach each other perpendicularly, and the reaction is nonsynchronous. The $\sigma(\mathrm{C}-\mathrm{C})$ distance in $\mathrm{TS}_{\mathrm{A}}(\mathbf{I X})$ is close to that in the product (a matter of $0.15 \AA$; Table S8).

Allene Addition to OCS vs Ketene Addition to Thioketene. Because the OCS molecule comprises three different atoms, the number of possible products in the course of the $[2+2]$ cycloaddition with allene is greater than that for analogous reactions of the $\mathrm{CX}_{2}$ molecules. The same holds true for the [2 $+2]$ cycloaddition of ketene and thioketene. Thus, four different four-membered-ring products can possibly be formed by OCS and allene reaction ( $\mathbf{X V}, \mathbf{X V I}, \mathbf{X X}$, and $\mathbf{X X I}$ ) and eight in ketene addition to thioketene (XVI, XVII, XVIII, XIX, XX, XXII, XXIII, and XXIV) (Figure 3).

Among the eight products formed possibly in the course of the $[2+2]$ cycloaddition of ketene and thioketene, three of them, namely XXII, XXIII, and XXIV, may be formed in endoergic reactions, whereas the remaining five may be formed in exoergic reactions (Chart 3, Tables S5 and S11). Note that the products in which the oxygen atom is built into the ring are positioned relatively high on the energy scale. Moreover, the two products that have both heteroatoms built into the ring (XXIII, XXIV) are the least stable. On the other hand, the most stable molecule XVI has the diketene skeleton in which the sulfur atom replaced the oxygen in the ring. Furthermore, XVI is the most favored because of the lowest energy barrier (21 $\mathrm{kcal} / \mathrm{mol}$; Chart 3, Tables S5 and S11). As for the thioketene dimerization reaction, the next lowest activation barrier is that toward XVIII (Figure S3), i.e., the product in which two heteroatoms are bound to the cyclobutane ring and are in the trans position. Also, 2-methylene-3-thietanone XVII, an analogue of $\mathbf{X}$, is the second most stable compound; however, as before, the barrier toward it is higher.

The transition state structures of the ketene-thioketene cycloadditions show the processes to be concerted, yet highly asynchronous (Figure 3, Table S10). Again, generally the $\sigma(\mathrm{C}-\mathrm{C})$ bond is formed first and either the $\sigma(\mathrm{C}-\mathrm{O})$ or the $\sigma(\mathrm{C}-\mathrm{S})$ bond is constituted next. In one case, however, the asynchronous pathway is not so obvious, because in $\mathrm{TS}_{\mathrm{B}}$ (XXIII) the proportions of the $\mathrm{C}-\mathrm{O}$ and $\mathrm{C}-\mathrm{S}$ distances are similar to those in the product. $\mathrm{TS}_{\mathrm{B}}(\mathbf{X V I I})$ and $\mathrm{TS}_{\mathrm{B}}(\mathbf{X X I I})$ look quite similar. Indeed, in these structures the $\sigma(\mathrm{C}-\mathrm{C})$ bond is almost formed and next either $\sigma(\mathrm{C}-\mathrm{O})$ or $\sigma(\mathrm{C}-\mathrm{S})$ is going to be constituted. However, in $\mathrm{TS}_{\mathrm{B}}(\mathbf{X V I I})$ (with the $\mathrm{C}-\mathrm{S}$ bond), the $\mathrm{C} 2-\mathrm{C} 3$ distance is greater by $0.2 \AA$ than that in $\mathrm{TS}_{\mathrm{B}}(\mathbf{X X I I})$, leading to a molecule with a much shorter $\mathrm{C}-\mathrm{O}$ bond in the ring. Furthermore, in $\mathrm{TS}_{\mathrm{B}}(\mathbf{X V I I})$, the $\mathrm{C}-\mathrm{S}$ distance is even shorter than the $\mathrm{C}-\mathrm{O}$ distance. Similarly to the thioketene dimerization, we found two different TS structures, $\mathrm{TS}_{\mathrm{B}}(\mathbf{X V I I})$


Figure 4. AIM analysis of the transition state structures for allene- $\mathrm{CO}_{2}$ (path A ) and ketene dimerization (path B ) reactions calculated at the MP2/aug-cc-pVDZ level. The bond critical points $(3,-1)$ are shown as either small balls (ordinary bonds) or open circles (newly formed bonds). The ring critical points $(3,+1)$ are shown as crossed open circles.
and $\mathrm{TS}_{\mathrm{B}}(\mathbf{X I X})$, of the same energy. As previously, this is due to mirror symmetry of these TS structures.

Only two, out of four, cycloaddition products formed by allene with OCS, carrying the S-atom built into the ring, seem to be thermodynamically stable. Yet their stability is as small as ca. $1 \mathrm{kcal} / \mathrm{mol}$ (Chart 3, Tables S5 and S11). Although energetic differences less than $1 \mathrm{kcal} / \mathrm{mol}$ are hardly interpretable, the energetic order of the structures with the $S$-atom in the ring, XV and XVI, is the same as for the analogous compounds VIII and IX, and the opposite order of $\mathrm{TS}_{\mathrm{A}}(\mathbf{X V})$ and $\mathrm{TS}_{\mathrm{A}}(\mathbf{X V I})$ (Figure S 3 ) reflects also the same tendency as for $\mathrm{TS}_{\mathrm{A}}(\mathbf{V I I I})$ and $\mathrm{TS}_{\mathrm{A}}(\mathbf{I X})$. On the other hand, the $\mathbf{X X}$ and XXI molecules, which have the O -atom built into the ring, exhibit an energetic order analogous to the allene with $\mathrm{CO}_{2}$ cycloaddition products. This holds true for the $\mathrm{TS}_{\mathrm{A}}(\mathbf{X X})$ and $\mathrm{TS}_{\mathrm{A}}(\mathbf{X X I})$ structures, too.

As for the allene $-\mathrm{CX}_{2}$ reactions, the TS leading to the 3-methylene isomers, $\mathrm{TS}_{\mathrm{A}}(\mathbf{X V})$ and $\mathrm{TS}_{\mathrm{A}}(\mathbf{X X I})$, are almost planar, whereas those leading to the 4 -methylene isomers, $\mathrm{TS}_{\mathrm{A}}(\mathbf{X V I})$ and $\mathrm{TS}_{\mathrm{A}}(\mathbf{X X})$, exhibit nonplanarity which is more pronounced in compounds with the S -atom than in those with the O -atom built into the ring. As before, the $\mathrm{TS}_{\mathrm{A}}$ structures indicate that the reaction path A is concerted and nonsynchronous. Also, inspection into the imaginary frequency interpretation (Table S5) confirms a simultaneous formation of the two bonds in the transition state structure along the reaction coordinate.

Summary of the Reaction Energetics. Comparison of the reaction energies and activation barrier heights in the systems studied (Charts $1-3$ ) allows us to conclude that the reactions of the allene molecule proceed through very high activation barriers and the products are thermodynamically stable very rarely: only the products that involve the sulfur atom built into the ring are stabilized slightly ( -0.7 to $-5.1 \mathrm{kcal} / \mathrm{mol}$ ). In the
allene reactions, the lowest activation barriers occur in the case of $[2+2]$ cycloaddition with $\mathrm{CS}_{2}$ and the highest in the case of $\mathrm{CO}_{2}$ addition. The lowest activation barriers in dimerization of ketene or thioketene are in the range of $20-30 \mathrm{kcal} / \mathrm{mol}$. Thus, these reactions run quite easily. It is noticeable that the more oxygen atoms participate in the reaction the higher is the barrier. The energy barrier tends to change in line with the HOMO-LUMO energy gap changes (Table S2). Note that the energy gaps of allene reactions are usually by ca. 2 eV larger than those for the (thio)ketene reactions. The products possibly formed in the reactions involving ketene and thioketene are thermodynamically stable, especially those that incorporate the sulfur atom in the ring.

Inspecting the allene molecule addition energetics allows us to summarize the results as follows:
(i) Among the products incorporating the S -atom built into the ring, the 3-methylene isomers are thermodynamically more stable than the 4-methylene isomers, whereas the energetic order of the activation barriers is opposite.
(ii) Among the products incorporating the O -atom built into the ring, the 4-methylene isomers are both thermodynamically and kinetically more stable than the 3 -methylene isomers.

In the reactions of (thio)ketene we observe again higher stabilities of the four-membered-ring products with the S -atom built into the ring. In this class of reactions, the most stable products are those that have a diketene skeleton which generally have the lowest activation barriers, too. In one case, however, the barrier height is lower for the diketene-like transition state, i.e., 1,3-cyclobutanedione ( $\mathrm{TS}_{\mathrm{B}}(\mathbf{I I})$ ). Its sulfur analogues have barriers as low as those for diketene-like analogues, XII and XVIII; however, they are thermodynamically less stable.

Summary of the TS Geometries. Several regularities can be found in the TS geometries for the subseries of analogues (Figures 1-3).


Figure 5. AIM analysis of the transition state structures for allene- $\mathrm{CS}_{2}$ (path A ) and thioketene dimerization (path B) reactions calculated at the MP2/aug-cc-pVDZ level. The bond critical points $(3,-1)$ are shown as either small balls (ordinary bonds) or open circles (newly formed bonds). The ring critical points $(3,+1)$ are shown as crossed open circles.
(i) The TSs leading to 3-methylene products (III, VIII, XV, and XXI) along reaction path $\mathrm{A}(\mathrm{XCY}+$ allene; $\mathrm{X}, \mathrm{Y}=\mathrm{O}, \mathrm{S})$, are nearly planar: the $\omega$ angle does not exceed $5^{\circ}$.
(ii) The TSs leading to 4-methylene products (I, XX, XVI, $\mathbf{I X}$ ) along reaction path A are nonplanar, and the ring deformation increases from $20^{\circ}\left(\mathrm{CO}_{2}\right)$, through $36^{\circ}(\mathrm{OCS}, \mathrm{O}$ in the ring) or $45^{\circ}$ (OCS, S in the ring), to $74^{\circ}\left(\mathrm{CS}_{2}\right)$.
(iii) The TSs leading to 4 -methylene products (I, XX, XVI, $\mathbf{I X})$ along reaction path $\mathrm{B}\left(\mathrm{H}_{2} \mathrm{CCX}+\mathrm{H}_{2} \mathrm{CCY} ; \mathrm{X}, \mathrm{Y}=\mathrm{O}, \mathrm{S}\right)$ are nonplanar as well, and the ring deformation $\omega$ increases from $-54^{\circ}(\mathrm{O}-\mathrm{C}=\mathrm{O})$, through $+58^{\circ}(\mathrm{O}-\mathrm{C}=\mathrm{S}, \mathrm{O}$ in the ring $)$ or $101^{\circ}\left(\mathrm{S}-\mathrm{C}=\mathrm{O}, \mathrm{S}\right.$ in the ring), to $106^{\circ}(\mathrm{S}-\mathrm{C}=\mathrm{S})$.
(iv) The TSs leading to cyclobutane ring substituted with heteroatoms at the trans position (II, XVIII, XII) obtained along path $B$ are nonplanar again; however, the deformation angle increases only very slightly from $45^{\circ}(\mathrm{O}=;=\mathrm{O})$, through $48^{\circ}$ $(\mathrm{O}=;=\mathrm{S})$, to $51^{\circ}(\mathrm{S}=;=\mathrm{S})$.
(v) The TSs leading to cyclobutane ring substituted with heteroatoms at the cis position (IV, XIX, XI) obtained along path B are nonplanar, and the $\omega$ angle increases from $-61^{\circ}$ $(\mathrm{O}=$; $=\mathrm{O})$, through $111^{\circ}(\mathrm{O}=;=\mathrm{S})$, to $122^{\circ}(\mathrm{S}=;=\mathrm{S})$.
(vi) The TSs leading to rings with two heteroatoms built in the 1,3-positions (VI, XXIII, XIII) (path B) are slightly nonplanar, and the $\omega$ angle increases from $-24^{\circ}$ ( $-\mathrm{O}-$; $-\mathrm{O}-)$, through $-14^{\circ}(-\mathrm{O}-;-\mathrm{S})$, to $0^{\circ}(-\mathrm{S}-;-\mathrm{S})$.
(vii) There is a decreasing trend in the $\omega$ angle for the subseries of TSs with the two heteroatoms built into the ring in the 1,2-positions (VII, XXIV, XIV) (path B): $0^{\circ}(-\mathrm{O}-\mathrm{O}-)$, $11^{\circ}(-\mathrm{O}-\mathrm{S}-)$, and $-62^{\circ}(-\mathrm{S}-\mathrm{S}-)$.
(viii) The tendency is not so regular for the TSs toward 2-methylene products (V, XXII, XVII, X). The $\omega$ angle changes
from $0^{\circ}(-\mathrm{O}-;=\mathrm{O})$, through $13^{\circ}(-\mathrm{O}-;=\mathrm{S})$, to $73^{\circ}(-\mathrm{S}-$; $=\mathrm{O})$, to $58^{\circ}(-\mathrm{S}-$; $=\mathrm{S})$.

The [2 +2 ] Cycloaddition Mechanisms. The following assumptions and reasons form the platform for our considerations of the reaction mechanism. We assumed the reactants to be in the fundamental singlet states, excluding simultaneously excitation of one of the reactants as a driving force for the reaction. When studying the reaction paths, we searched for more than one TS (required for the reaction to be two step or multistep). However, we always ended up with one TS. Although in performing the unrestricted MP2 calculations we looked for triplet TSs, we have never found one: all the optimizations of a TS structure in a triplet state either did not converge or converged to the products in their triplet states. Finally, some authors considered zwitterionic TSs; ${ }^{39}$ however, inspection into the partial charge distribution (fitted to the electrostatic potential) ${ }^{40}$ shows more than a two-center charge separation in the TSs. According to the above assumptions and argumentation, the reaction mechanisms considered are in the frame of concerted (one-step) reactions with the singlet TS structures.

The Woodward-Hoffmann rules ${ }^{14}$ refer to symmetry of the reactants, symmetry of HOMO-LUMO orbitals, and their conservation throughout the reaction. The vast majority of the TSs studied show the reactions to be concerted and asynchronous. For all the TSs studied we performed AIM analysis of the electron density and found all the bond critical points $(3,-1)$ and the ring critical point $(3,+1)$. We stress that the present analysis yields an electron density picture for pericyclic and pseudopericyclic reactions that does not use the orbital-base picture of bonding. We made the assumption that


Figure 6. AIM analysis of the transition state structures for allene-OCS reaction (path A) and ketene addition to thioketene (path B) calculated at the MP2/aug-cc-pVDZ level. The bond critical points $(3,-1)$ are shown as either small balls (ordinary bonds) or open circles (newly formed bonds). The ring critical points $(3,+1)$ are shown as crossed open circles.
the presence of two new bond critical points (BCPs; in comparison to the number of BCPs in reactants), between the atoms in a TS that had to be connected by a new $\sigma$-bond, indicated a pericyclic type of $[2+2]$ cycloaddition, which always was additionally confirmed by the presence of the ring critical point (RCP). On the other hand, the presence of only one new BCP (always accompanied by the absence of an RCP) suggested a pseudopericyclic type of the reaction. The next problem appears, however. Only some of the TSs are planar as needed for the reaction to be classified as pseudopericyclic. ${ }^{20 b}$ The reactions with TSs that are nonplanar and exhibit discontinuity can be classified as neither pericyclic nor ordinary pseudopericyclic. The latter type of the reaction we call here the nonplanar-pseudopericyclic (NP-pseudopericyclic) reaction. Now another (smaller) problem arises: which TS ring nonplanarity is sufficient for the reaction to be classified as NPpseudopericyclic? Some authors classified the reaction with TS nonplanarity of ca. $30^{\circ}$ as pseudopericyclic. ${ }^{23 \mathrm{~d}}$ Here, we arbitrarily accept the TS nonplanarity from $-45^{\circ}$ to $+45^{\circ}$ for the reaction to be classified as pseudopericyclic, and thus the NP-pseudopericyclic is the reaction with the discontinuity and ring nonplanarity over $45^{\circ}$. Last, but not least, in two cases (namely $\mathrm{TS}_{\mathrm{B}}(\mathbf{V})$ and $\mathrm{TS}_{\mathrm{A}}(\mathbf{V I I I})$ ), the new BCP and RCP indicate hydrogen-bond-like interaction ${ }^{41}$ in the TS rather than $\sigma$-bond formation. Those critical points were ignored in the classification of the reaction mechanism.

Following the above argumentation, the allene cycloadditions with the $\mathrm{X}=\mathrm{C}=\mathrm{Y}$ molecules to the most stable products, I, VIII, and $\mathbf{X V}$ are pericyclic (Figures $4-6$ ). The pericyclic mechanism is also revealed for the reactions through $\mathrm{TS}_{\mathrm{A}}(\mathbf{I I I})$ and
$\mathrm{TS}_{\mathrm{A}}(\mathbf{X V I})$ (Figures 4-6). On the other hand, reaction path A is pseudopericyclic for $\mathbf{X X}$ and $\mathbf{X X I}$, because the $\mathrm{TS}_{\mathrm{A}}(\mathbf{X X})$ and $\mathrm{TS}_{\mathrm{A}}(\mathbf{X X I})$ exhibit ring deformation smaller than $45^{\circ}$. Finally, the cycloadditions toward IX are NP-pseudopericyclic, since for the lowest barrier at path $\mathrm{A}, \mathrm{TS}_{\mathrm{A}}(\mathbf{I X})$, the ring deformation angle is equal to $-73.6^{\circ}$.

Generally, the (thio)ketene cycloadditions can be classified as NP-pseudopericyclic. Indeed, $\mathrm{TS}_{\mathrm{B}}(\mathbf{I}), \mathrm{TS}_{\mathrm{B}}(\mathbf{I I}), \mathrm{TS}_{\mathrm{B}}(\mathbf{I V})$, $\mathrm{TS}_{\mathrm{B}}(\mathbf{I X}), \mathrm{TS}_{\mathrm{B}}(\mathbf{X}), \mathrm{TS}_{\mathrm{B}}(\mathbf{X I}), \mathrm{TS}_{\mathrm{B}}(\mathbf{X I I}), \mathrm{TS}_{\mathrm{B}}(\mathbf{X I V}), \mathrm{TS}_{\mathrm{B}}(\mathbf{X V I})$, $\mathrm{TS}_{\mathrm{B}}(\mathbf{X V I I}), \mathrm{TS}_{\mathrm{B}}(\mathbf{X V I I I}), \mathrm{TS}_{\mathrm{B}}(\mathbf{X I X})$, and $\mathrm{TS}_{\mathrm{B}}(\mathbf{X X})$ are very nonplanar and possess only one additional BCP. In particular, reactions toward the most stable products and through the lowest barriers II, IX, and XVI are NP-pseudopericyclic. The other cycloadditions at path B, but toward $\mathbf{V}$ and XXII, are pericyclic. Indeed, each of $\mathrm{TS}_{\mathrm{B}}(\mathbf{V I}), \mathrm{TS}_{\mathrm{B}}(\mathbf{V I I}), \mathrm{TS}_{\mathrm{B}}(\mathbf{X I I I}), \mathrm{TS}_{\mathrm{B}}(\mathbf{X X I I I})$, and $\mathrm{TS}_{\mathrm{B}}$ (XXIV) exhibits two new BCPs and one RCP (Figures $4-6) . \mathrm{TS}_{\mathrm{B}}(\mathbf{X X I I})$ is nearly planar and exhibits only one additional BCP; thus the reaction is pseudopericyclic. $\mathrm{TS}_{\mathrm{B}}(\mathbf{V})$ is an exception because three new BCPs and two RCPs appear. However, two of the BCPs and both RCPs are due to hydrogen-bond-like interaction in the transition state. As only one of the new BCPs corresponds to the newly formed $\sigma$-bond and the TS structure is planar, the reaction can be classified as pseudopericyclic.

## Conclusions

A comprehensive theoretical MP2/aug-cc-pVDZ study was performed on the [ $2+2$ ] cycloaddition of allene with XCY as well as $\mathrm{H}_{2} \mathrm{CCX}$ with $\mathrm{H}_{2} \mathrm{CCY}(\mathrm{X}, \mathrm{Y}=\mathrm{O}, \mathrm{S})$ leading to all
possible four-membered products. Attention has been focused especially on the transition state structures and energetics. It has been established that the reactions of the allene molecule proceed through very high activation barriers and the products are thermodynamically stable when the S -atom is built into the four-membered ring. Several products are possible when the $\mathrm{H}_{2} \mathrm{CCX}$ molecule is cycloadded to the $\mathrm{H}_{2} \mathrm{CCY}$ one; however, some of the reactions (for example, toward 4-methylene-2oxetanone, 1,3-cyclobutanedione, 4-methylenethietane-2-thione, 1,3-cyclobutanedithione, or 4-methylenethietan-2-one) are predicted to run easily, i.e., with activation energies of ca. 20-30 $\mathrm{kcal} / \mathrm{mol}$. Generally, for the two kinds of reactions the more oxygen atoms participate in the reaction the higher is the barrier. The energy barrier tends to change in line with the HOMOLUMO reactant energy gap changes. Except for planar TS structures leading to the 3-methylene products, during the reaction of the allene with XCY, most of the TSs are nonplanar. Generally, the more sulfur atoms participate the more nonplanar the TS is. All the studied reactions are concerted and asynchronous. The AIM analysis of the electron density distribution in the TS structures allowed distinguishing pericyclic from pseudopericyclic from nonplanar-pseudopericyclic types of reaction.

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Supporting Information Available: Table S1, schematic structures, molecule numbering, and names of the system studied. Table S2, HOMO-LUMO energy gaps for the reactants. Tables S3-S11, detailed MP2/aug-cc-pVDZ calculated geometries as well as MP2/aug-cc-pVDZ energies, energies corrected for ZPE, and Gibbs free energies for all products and appropriate transition structures considered in this paper. Figures S1-S3, IRC profiles for reactions toward the most stable products. This material is available free of charge via the Internet at http://pubs.acs.org.

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